Accelerating Advection Via Approximate Block Exterior Flow Maps

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Abstract

Flow visualization techniques involving extreme advection workloads are becoming increasingly popular. While these techniques often produce insightful images, the execution times to carry out the corresponding computations are lengthy. With this work, we introduce an alternative to traditional advection, which improves on performance at the cost of decreased accuracy. Our approach centers around block exterior flow maps (BEFMs), which can be used to accelerate flow computations by reducing redundant calculations. Our algorithm uses Lagrangian interpolation, but falls back to Eulerian advection whenever regions of high error are encountered. In our study, we demonstrate that the BEFM-based approach can lead to significant savings in time, with limited loss in accuracy.

Introduction

A myriad of scientific simulations, including those modeling fluid flow, astrophysics, fusion, thermal hydraulics, and others, model phenomena where constituents move through their volume. This movement is captured by a velocity field stored at every point on the mesh. Further, other vector fields, such as force fields for electricity, magnetism, and gravity, also govern movement and interaction. A wide range of flow visualization techniques are used to understand such vector fields. The large majority of these techniques rely on placing particles in the volume and analyzing the trajectories they follow. Traditionally, the particles are displaced through the volume using an advection step, i.e., solving an ordinary differential equation using a Runge-Kutta integrator.

As computational power on modern desktops has increased, flow visualization algorithms have been empowered to consider designs that include more and more particles advecting for longer and longer periods. Techniques such as Line Integral Convolution and Finite-Time Lyapunov Exponents (FTLE) seed particles densely in a volume and examine where these particles end up. For these operations, and many others, only the ending position of the particle is needed, and not the details of the path the particle took to get there.

Despite seemingly abundant computational power, some techniques have excessively long running times. For example, ocean modelers often study the FTLE within an ocean with both high seeding density and very long durations for the particles (years of simulation time) \([2, 3]\). As another example, fusion scientists are interested in FTLE computations inside a tokamak where particles travel for hundreds of rotations \([1]\). In both cases, FTLE calculations, even on supercomputers, can take tens of minutes.

With this work, we consider an alternative to traditional Eulerian advection. The key observation that motivates the work is that, in conditions with dense seeding and long durations, particles will tread the same (or very similar) paths over and over. Where the current paradigm carries out the same computation over and over, we consider a new paradigm where a computation can be carried out a single time, and then reused. That said, we find that, while particle trajectories do often travel quite close to each other, they typically follow their own (slightly) unique paths. Therefore, to effectively reuse computations, we consider a method where we interpolate new trajectories from existing ones, effectively trading accuracy for speed.

Our method depends on Block Exterior Flow Maps, or BEFMs. The idea behind BEFMs is to pre-compute known trajectories that lie on block boundaries. It assumes data in block-decomposed, but this assumption is common when dealing with parallel, distributed-memory computations. When a compute-intensive flow visualization algorithm is then calculated, it consults with the BEFMs and does Lagrangian-style interpolation from its known trajectories. While this approach introduces error, it can be considerably faster, since it avoids Eulerian advection steps inside each block.

The contributions of the paper are as follows:

- Introduction of BEFMs as an operator for accelerating dense particle advection calculations;
- A novel method for generating an approximate BEFM that can be used in practice;
- A study that evaluates the approximate BEFM approach, including comparisons with traditional advection.

Related Work

McLouglin et al. recently surveyed the state of the art in flow visualization \([4]\), and the large majority of techniques they described incorporate particle advection. Any of these techniques could possibly benefit from the BEFM approach, although the tradeoff in accuracy is only worthwhile for those that have extreme computational costs, e.g., Line Integral Convolution \([5]\), finite-time Lyapunov exponents \([6]\), and Poincare analysis \([7]\).

One solution for dealing with extreme advection workloads is parallelization. A summary of strategies for parallelizing particle advection problems on CPU clusters can be found in \([8]\). The basic approaches are to parallelize-over-data, parallelize-over-particles, or a hybrid of the two \([9]\). Recent results using parallelization-over-data demonstrated streamline computation on up to 32,768 processors and eight billion cells \([11]\). These parallelization approaches are complementary with our own. That is, traditional parallel approaches can be used in the current way, but the phase where they advect particles through a region could be replaced by our BEFM approach.
In terms of precomputation, the most notable related work comes from Nouanesengsy et al. [10]. They precomputed flow patterns within a region and used the resulting statistics to decide which regions to load. While their precomputation and ours have similar elements, we are using the results of the precomputation in different ways: Nouanesengsy et al. for load balancing and ourselves to replace multiple integrations with one interpolation.

In terms of accelerating particle advection through approximation, two works stand out. Brunton et al. [18] also looked at accelerating FTLE calculation, but they considered the unsteady state problem, and used previous calculations to accelerate new ones. While this is a compelling approach, it does not help with the steady state problem we consider. Hilwatsh et al. [15] employ an approach where flow is calculated by following hierarchical lines. This approach is well-suited for their use case, where all data fits within the memory of a GPU, but it is not clear how to build and connect hierarchical lines within a distributed memory parallel setting. In contrast, our method, by focusing on flow between exteriors of blocks, is well-suited for this type of parallelism.

Bhatia et al. [19] studied edge maps, and the properties of flow across edge maps. While this work clearly has some similar elements to our, their focus was more on topology and accuracy, and less on accelerating particle advection workloads.

Scientific visualization algorithms are increasingly using Lagrangian calculations of flow. Jobard et al. [12] presented a Lagrangian-Eulerian advection scheme which incorporated forward advection with a backward tracing Lagrangian step to more accurately shift textures during animation. Salzbrunn et al. delivered a technique for analyzing circulation and detecting vortex cores given predicates from pre-computed sets of streamlines [14] and pathlines [13]. Agranovsky et al. [16] focused on extracting cores given predicates from pre-computed sets of streamlines [14]. Agranovsky et al. [16] focused on extracting cores given predicates from pre-computed sets of streamlines [14]. Lekschas et al. [16] focused on extracting cores given predicates from pre-computed sets of streamlines [14]. Lekschas et al. [16] focused on extracting cores given predicates from pre-computed sets of streamlines [14].

Method

Our method makes use of block exterior flow maps (BEFM). We begin by defining this mapping, in Section . We then describe our method, and how it incorporates these maps, in Section .

Block Exterior Flow Map
Definition

In scientific computing, parallel simulation codes often partition their spatial volume over their compute nodes. Restated, each compute node will operate on one spatial region, and that compute node will be considered the “owner” of that region. Such a region is frequently referred to as a block. For example, a simulation over the spatial region X: [0-1], Y: [0-1], and Z: [0-1] and having N compute nodes could have N blocks, with each block covering a volume of \( \frac{1}{N} \).

Consider a point \( P \) that lies on the exterior of a block \( B \). If the velocity field points toward the interior of \( B \) at point \( P \), then Eulerian advection of a particle originating at \( P \) will take the particle through the interior of \( B \) until it exits. In this case, the particle will exit \( B \) at some location \( P' \), where \( P' \) is also located on the exterior of \( B \). The BEFM captures this mapping. The BEFM’s domain is all spatial locations on the exterior of blocks, and its range is also spatial locations on the exteriors of blocks. Further, for any given \( P \) in the BEFM’s domain, \( \text{BEFM}(P,B) \) will produce a location that is on \( B \)‘s exterior. Saying it concisely, the BEFM is the mapping from particles at exteriors of blocks to the locations where those particles will exit the block under Eulerian advection. Figure 1 illustrates an example of a BEFM.

Using BEFMs for Calculating Particle Trajectories

Now consider a particle \( P \) that lies on the interior of block \( B_0 \). Further, consider the trajectory of \( P \) when traveling for \( T \) time units. Assume \( P \) travels through blocks \( B_1, B_2, ..., B_{N-1} \), before terminating in the interior of block \( B_N \) at time \( T \). Consider how BEFMs can be used to calculate \( P \)’s trajectory:

- Since \( P \) lies in the interior of \( B_0 \), traditional advection is needed to calculate the path of \( P \) until it reaches \( B_0 \)’s exterior.
- The BEFM can then be used to calculate the path of \( P \) through \( B_1, B_2, ..., B_{N-1} \).
- \( P \)’s trajectory into the interior of \( B_N \) is then again calculated with traditional advection.

Putting it all together, if BEFMs can calculate mappings more quickly than the calculations for advecting a particle through a block, then this method should be faster than traditional advection. Further, the speedup for the BEFM-style calculation is then limited only by the cost for the steps through the initial and final blocks (\( B_0 \) and \( B_N \)).

Approximate BEFMs

There are many ways to implement a BEFM. For example, a BEFM could respond to each mapping request (i.e., a \( \text{BEFM}(P,B) \)) by going back to the original vector field and employing traditional advection. In this case, the BEFM would have the same performance characteristics as traditional advection, and the abstraction of BEFMs on top of traditional advection would be unnecessarily complicated.
For our research, we are interested in BEFMs where each mapping request can be satisfied much more quickly than the work it takes to advect a particle using traditional advection. For this reason, we consider precomputation, i.e., evaluating the BEFM before the main work begins of calculating particle trajectories. However, it is not obvious how to precompute a perfect BEFM. Our approach to this problem is to precompute an Approximate BEFM or ABEFM. This ABEFM will know the exact mappings for certain locations on the boundary. We refer to this list of locations as the KnownParticleList.

When an ABEFM is asked to calculate mappings for particles that are not in the KnownParticleList, it will interpolate the exit location from the nearest particles that are in the KnownParticleList.

There are many ways to establish an ABEFM’s KnownParticleList. We chose to generate locations uniformly along the exterior of a block at some chosen sample density. With this approach, the accuracy and pre-computation time are in tension. High sample densities will increase accuracy at the cost of pre-computation time. Low sample densities will reduce pre-computation time at the cost of accuracy. We explore this issue more in Section 3.1.2.

Conditions Where an ABEFM Cannot Be Used

It is not always possible to interpolate new trajectories from the ABEFM’s known trajectories. Through our experiments, we have identified three ways in which interpolation is not possible. They are:

1. If a particle trajectory from the exterior of block B never again reaches the exterior of block B, i.e., if a particle lands in a sink or is caught in a vortex inside the block.
2. If a particle trajectory differs too significantly from its neighbors, i.e., neighboring trajectories separated and exit through different faces of B.
3. If all neighboring trajectories are not uniformly entering the block or uniformly exiting the block, e.g., some neighboring particles get displaced to the interior of the block while others are displaced into neighboring blocks.

Building an ABEFM

ABEFM construction consists of generating flows for each location in the KnownParticleList. This is done by initializing particles at each location in the KnownParticleList and then advecting those particles across a block. Advection is done using traditional Eulerian methods such as Runge-Kutta. Pseudo code for this method is outline in Algorithm 1.

Algorithm 1 Build Flow Map
1: function GET BLOCK ID(Particle P)
2: Determine the block that P advects through
3: return BlockID
4: end function
5: function ADVECT ON BLOCK(Particle P, Block B)
6: Advect P until it exits B (using Eulerian advection)
7: Stop P on boundary of B
8: Compute which Face of B that P landed on
9: return P, FaceID
10: end function
11: for all P in KnownParticleList do
12: Bid = GET BLOCK ID(P)
13: NewP, Fid = ADVECT ON BLOCK(P, Bid)
14: Def: Flow F as the set < P, NewP, Bid, Fid >
15: end for

Advecting With an ABEFM

Section 3.1.2 describes how to use a BEFM for particles at arbitrary locations in a volume. For this discussion, we focus on the case of a particle P that lies on the boundary of block B, and calculating where P exits B.
The trajectory for a particle \( P \) is calculated as follows. First, the neighboring particles, \( P_1, P_2, \ldots, P_n \) from the Known ParticleList are identified. For our study, the Known ParticleList had particles seeded at regular intervals, so \( n \) would be four, and we would find the four particles that formed a square around \( P \). Next, we check the \( P_i \) for our three conditions where an ABEFM cannot be used (see 3.1.4). If we cannot use the \( P_i \), then we fall back to traditional Eulerian advection using Runge-Kutta solves. If we can use the \( P_i \), then we take the output location to be the weighted average of the exit locations of the \( P_i \). For our construction of four \( P_i \)'s in a square configuration, this can be accomplished with bilinear interpolation. We also interpolated the trajectory for a particle \( P \) is calculated as follows. First, \( P \) is on boundary of \( B \), we considered three data sets. Each had steady state flow (i.e., one time slice) and was defined on a regular mesh. They are:

- **Tokamak**: the magnetic field inside a tokamak. Inside the tokamak, the velocity vector values lead to circulation around the tokamak. Outside the tokamak, the velocity field is all zero vectors. This data set had dimensions \( 300^3 \).
- **Astro**: a supernova simulation. The vector field has high variability in its central spherical region, and steadily points out or in when approaching the edges. This data set had dimensions \( 256^3 \).
- **TH**: a thermal hydraulics simulation of air mixing in a “fish tank” box with two inlets — one with hot air and one with cold air — and an outlet. This data set had dimensions \( 500^3 \).

**Testing Factors**

We considered six dimensions of configurations:

- **Domain block layout**: what are the impacts of having fewer or more blocks?
- **Density of known particles**: what are the impacts in calculating more or less particles during preprocessing? — time for preprocessing, time for regular execution, and accuracy?
- **Integration time**: how does performance and accuracy change as particles go for shorter or longer periods?
- **Step size**: how does step size affect performance and accuracy?
- **Data set**: how does the underlying vector field affect performance and accuracy?

**Testing Methodology**

Our methodology consisted of seven phases. The first phase studied our “default” case in detail. Each of the remaining six phases sweep through one dimension of our testing factors, and explores the impact of that factor.

**Phase 1: Baseline Test**

Our Baseline case consists of a workload, and a configuration for ABEFM. The default workload was a mesh resolution number of particles integrating for 10 time units with a step size of 0.001 on the vector field from the Tokamak data set. The default ABEFM configuration on the Tokamak was \((10x10x10)\) blocks and 300 particles precomputed in each dimension for the Known ParticleList.

**Phase 2: Block Layout**

With this phase, we wanted to understand the effects of changing block size. Large blocks cause particles to travel larger distances, but the interpolated path may be less accurate. Small blocks cause particles to travel shorter distances — and so the number of operations needed to go the same distance is greater — but the interpolated path may be more accurate. With this phase, we wanted to understand the magnitude of these effects.

We considered 9 block layouts: \((5x5x5)\), \((10x10x10)\), \((15x15x15)\), \((20x20x20)\), \((25x25x25)\), \((30x30x30)\), \((40x40x40)\), \((50x50x50)\), and \((100x100x100)\). Additionally we use the outcome from this phase to focus a more detailed look at a few more layouts.

**Phase 3: Integration Time**

With this phase, we considered integration time. Short integration times imply that we spend the majority of our time using traditional advection to get to block boundaries, mitigating the opportunity for speedup. Longer integration times, however, create

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**Algorithm 2 Advect with Flow Map**

1: function ADVECT BLOCK(\( Particle \ P \), \( Block \ B \))
2: Integrate to find \( P \)'s exit location
3: Set \( P \) on boundary of \( B \)
4: if \( P.Time \geq \) End Time then
5: return 0
6: else
7: return 1
8: end if
9: end function
10: function ADVECT VIA FLOW MAP(\( Particle \ P \), \( Block \ B \))
11: Interpolate Output location and time from (\( PB \))
12: if Output.Time > End Time then
13: return ADVECT BLOCK(\( P,B \))
14: end if
15: Set \( P = \text{Output} \)
16: return 1
17: end function
18: AdvectionList: List of particles to be advected
19: for all \( Particles \ P \) in AdvectionList do
20: keepGoing = 1
21: while \( P.Time < \) End Time && keepGoing do
22: Bid = GET BLOCK ID(\( P \))
23: if Particle on Computable Face then
24: keepGoing = ADVECT VIA FLOW MAP(\( P,Bid \))
25: else
26: keepGoing = ADVECT BLOCK(\( P,Bid \))
27: end if
28: end while
29: end for
the potential for applying the ABEFM repeatedly, and possibly significant speedups.

We considered 5 integration times: 1, 5, 10, 25, and 50 time units.

**Phase 4: Step Size**

With this phase, we considered step size. Small steps sizes move more slowly through a volume, while large step sizes move more quickly. However, for the ABEFM method, the step sizes only impact performance for stepping to the boundary, so the principal change is in the comparison with traditional advection.

We considered 7 step sizes: 0.1, 0.05, 0.01, 0.005, 0.001, 0.0005, and 0.0001.

**Phase 5: Density of Known Particles**

With this phase, we wanted to understand the effects of changing the number of known particles in the precomputation phase. Increasing this density will increase accuracy and the ability to use an ABEFM, but also increases precomputation costs. Decreasing this density could impact accuracy and decrease the ability to use an ABEFM, but reduces precomputation costs. With this phase, we again wanted to understand the magnitude of these effects.

We considered 5 densities along each dimension of the mesh: 100, 200, 300, 400, and 500.

**Phase 6: Data Set**

The performance of the ABEFM can clearly be affected by the underlying vector field. With this phase, we considered all three data sets. We performed the study from Phase 2 on each of the data sets keeping the total number of Eulerian steps constant. The Tokamak data set values are already listed in phase 2. The Astro data set used an integration time of 5000 and a step size of 1. The TH data set used the same configuration as the Tokamak data set. Each data set used their own native resolution for pre-computed particles for the KnownParticleList: 256 for Astro and 500 for FH. Each considered workloads of 20^9 particles.

**Phase 7: Accuracy Performance Comparison**

It is important to compare the accuracy and performance results of the ABEFM method with the traditional method. Since the traditional method already uses accuracy and performance tradeoffs we need to understand how this trade off compares with that of the ABEFM. For this study we hold the comparison step size fixed at 0.0001/ We then run a series of Euler and ABEFM runs at different step sizes to compare the resulting differences in accuracy and performance. In doing this we will be able to understand the region of performance and accuracy where the ABEFM method will out perform the traditional approach.

**Hardware**

All studies were performed on a machine with dual 8-core 3.2GHz E5-2667 v3 Intel Xeon processors and 132 GB of RAM. This initial study was done in use a single node, using 16 cores, with OpenMP parallelism over particles. We wished to enable the most direct comparisons between the ABEFM approach and traditional Eulerian integration methods so parallelism of each scheme was simplified to only OpenMP and looping over particles in each advection routine.

<table>
<thead>
<tr>
<th>Phase 1: Baseline Test Analysis</th>
<th>Measurement</th>
<th>Results</th>
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<tr>
<td></td>
<td>Absolute Error</td>
<td>Results from Phase 1.</td>
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<td>Max Error</td>
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<td></td>
<td>StdDev Error</td>
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**Measurments**

The measurements we took for each experiment were:

- Time: the total run time of the ABEFM approach (meaning both build time and advection time using the ABEFM). We also would run a separate experiment with the traditional, Eulerian approach and measure its time.
- Speedup: the total speed up from using an ABEFM compared to just Eulerian integration.
- Usability Metric: the percentage of time spent interpolating with the ABEFM versus using Eulerian integration and the percentage faces that an ABEFM can be used.
- Error: the average percent error and average displacement distance of an FTLE computed with the ABEFM advected particles with respect to the Eulerian advected particles. Differences in FTLE are used as the error metric since one of the leading motivations for ABEFMs use is the FTLE.

**Results**

**Phase 1: Baseline Test Analysis**

Phase 1 explores a single configuration, to set baseline expectations for the ABEFM method, and how the ABEFM method compares with traditional Eulerian advection. Table 1 shows the key results gathered in our study.

This baseline test demonstrates the viability of the ABEFM approach. Although the precomputation is non-trivial, it is still much smaller than the time to perform Eulerian advection. Additionally, the errors incurred were minimal — With the average less than 1% different from the Eulerian value. Figure 4 shows the FTLE computed using both the ABEFM method and traditional Eulerian advection showing that ABEFM version maintains all visible features distinguishable in the original Eulerian version.

**Phase 2: Varying Domain Block Layouts**

This phase studies the effect on ABEFM calculations when dividing the mesh into different numbers of blocks. Figure 5 shows tradeoffs in accuracy and speedup as the number of blocks increases. It shows that with the lowest number of blocks, both speedup and accuracy is quite good. By increasing the number of blocks, our accuracy drops off slightly and our run time slowly increases as the number of ABEFM jumps required to travel the same distance increases.
This configuration confirms that fastest run times with the Tokamak data set come from the block layouts with smaller numbers. In Figure 6 we look closer at block layouts based on the data set symmetry. Due to the cyclic nature of the data in the x and y dimensions we reduced the number of blocks in the z dimension and varied only the x and y dimensions. Before these studies, our initial intuition was that the closer the block jumps are the less error there will be, but this was not true here. Having less block jumps can also decreases the error as there are less interpolations that are approximating the flows locations and/or there is a greater percent of Eulerian updates. This displays a trade-off between the number of times an error is introduced versus the size of the errors introduced.

**Phase 3: Integration Time**

This phase looked at performance and accuracy as particles were allowed to travel for longer and longer distances. Figures 7 and 8 show the results of this study. The take away from these figures is that, as integration time increases, the speedups from the ABEFM method become increasingly higher. While this is expected, the study shows the extent of speedup that is possible. Speedup is ultimately limited by the number of faces along a block that can be used for interpolation (and thus do not have to fall back to Eulerian advection). The choice to fall back to Eulerian advection produces an Amdalh’s Law effect in our speedups as we get to higher and higher values of integration time.

**Phase 4: Step Size**

This phase varied the step size used for computing the Eulerian advection steps. This is used in building the BEFM and for all advections using the traditional Eulerian method. Figures 9 and 10 show the results of this phase.

Step size affects both the Eulerian method and the Eulerian portions of the ABEFM preprocessing phase. As step size decreases, the speedup increases, although it appears to be bound.

**Phase 5: Varying the KnownParticleList**

Phase 5 varied the density of the KnownParticleList. Figure 11 shows the affect on accuracy and performance when this factor is varied. For this test, the average accuracy decreases more significantly as we vary the density below the mesh resolution and
increases only gradually as we vary above the density of the mesh resolution. Additionally, the time to build the ABEFM increases with the increase in density of this list though not significantly as this range spanned a time of 0.33 seconds at 100 points per dimension and 4.33 seconds at 400 points per dimension, growing steadily in between. Our increase in performance and therefore our increasing speedups are accounted for by the larger number of acceptable BEFM jumps that can be preformed at the higher densities with less increase in performance as we reach the point where we stop improving our mapping significantly.

Phase 6: Varying the Data Set

This study incorporated the remaining two data sets (TH and Astro) to see how well they performed compared to the Tokamak data set. The data sets were studied with a variety of blocks (i.e., the same study that was performed in Phase 2, but for these new data sets). For reference, the Tokamak data set's results for this analysis were listed in Figure 5.

In the Astro data set, there is significant mixing in the center and headed straight out or straight in on the edges. The result of varying block dimension can be seen in Figure 12. It shows an optimal layout for run time at around $20^3$ resolution of blocks. The accuracy at this level is not significantly different then at other block sizes. This data set shows significantly less performance benefits as there are fewer blocks that have acceptable mappings for the ABEFM approach.

The second data set, TH, captures the mixing of hot and cold air currents. The vector field for this data set has significant mixing throughout its volume. The results of varying block dimension can be seen in Figure 13. The optimal layout for runtime is at around a block resolution of $20^3$. For this problem we do not see a significant affect on accuracy with a change in the block layouts.

Phase 7: BEFM vs. Euler

The ABEFM method has makes a tradeoff between accuracy and performance. Such a tradeoff is possible already within the traditional Eulerian approach, by increasing step size. In our final
phase, we compare our approach with increased step sizes using the traditional approach.

Figure 14 shows significant drop off in accuracy with the traditional method faces as step size increases, compared to the relatively small decrease in accuracy seen in the ABEFM method for the same changes. Figure 5 additionally shows that the ABEFM method reaches and maintains a higher speedup for all reasonable choices of the step size. The performance gains of the ABEFM method begin immediately as step size increases, while maintaining a relatively accurate calculation. The Eulerian method however suffers from a immediate drop in accuracy while not seeing any performance benefits until much further from the baseline step size. In the long run the Eulerian method is more affected by the change in step size and so gains a significant speed improvement but by this point has given up a significant amount of accuracy to do so.

Conclusion and Future Work

We introduced Block Exterior Flow Maps (BEFMs) and designed an algorithm for accelerating flow calculations using Approximate BEFMs (ABEFMs). The approach has two significant controlling parameters — block layout and density of known particles calculated in the preprocessing phase — and we studied the impacts of these parameters for multiple particle advection workloads. We found that ABEFMs provided significant winnings for extreme particle advection workloads, with one workload completing in 159 seconds where the traditional approach took 3,320 seconds, a speedup of more than 20X and with an average error of less than 2%. Further, as particles are advected for longer and longer distances, our technique has the possibility to show even greater gains.

This technique was developed in response to needs within the fusion community to advect for long periods around a tokamak. They are interested in the steady-state problem, so that is all we considered in this initial work. While our technique is currently useful for stand-alone post hoc analysis, our future work will be to insert the method into their simulation codes for in situ processing. While our preprocessing times are currently large, we believe they can be accelerated on the many-core architectures now prevalent on top supercomputers. Further, our block-centric approach lends itself well to distributed memory parallelism. In another branch of future work, we would like to consider constructing the ABEFM adaptively, in an effort to minimize unnecessary calculations, and to increase resolution in complex flow regions.

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